

HYPOTHESIS TEST

Suppose you want to determine whether the mean content of Supercola cans is less than 12 oz

Hypothesis Test

Trial by Jury

Supercola cans

Accused

Researchers

Prosecution

Data

Evidence

Claim: $\mu < 12$

Charges against the accused

We assume that the claim is not true

Charges are assumed to be not true

until we have sufficient evidence to the contrary

until proven otherwise beyond reasonable doubt

$$n = 50$$

$$\bar{x} = 11.7$$

$$s = 1$$

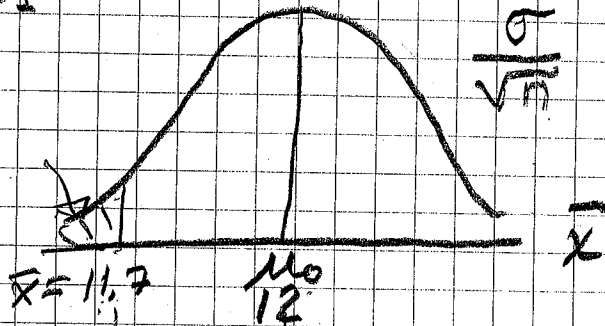
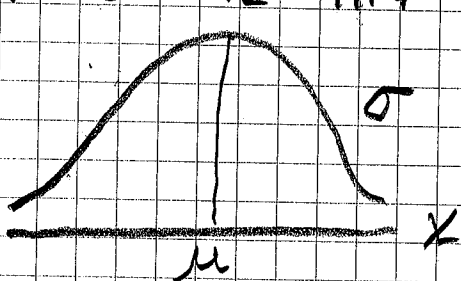
Assume

$$H_0: \mu = 12$$

Claim

$$H_a: \mu < 12$$

$n = 50$ $\bar{x} = 11.7$ $s = 1$



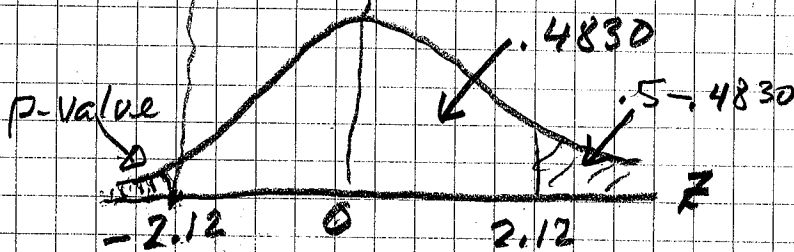
$H_0: \mu = 12$

$H_a: \mu < 12$

~~$Z = \frac{x - \mu}{\sigma}$~~

$$Z = \frac{\bar{x} - \mu_0}{\sigma / \sqrt{n}}$$

Test statistic



$$Z = \frac{11.7 - 12}{1 / \sqrt{50}} = -2.12$$

$p\text{-value} = .5 - .4830 = .017$

and that is the probability of getting a sample mean of 11.7 or farther to the left, assuming that $\mu_0 = 12$

that is a very small probability!

(A very unlikely event)

Reject H_0 and conclude H_a

$\alpha = .05$ the level of significance

$\alpha = .01, .10$

Decision Rule:

" If $p\text{-value} < \alpha$, reject H_0
and conclude H_a "

Conclusion:

" The data provide sufficient
evidence to conclude that all
Supercola cans have a mean content
less than 12 oz"

Summary

Step 1

Set up H_0 :
 H_a :

Step 2

Test statistic

Step 3

P-value

Rejection Regions

Step 4

Decision

Step 5

Conclusion

, at $\alpha = .05$