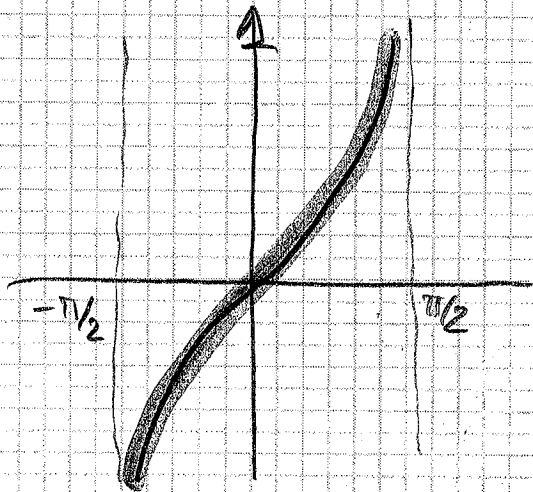
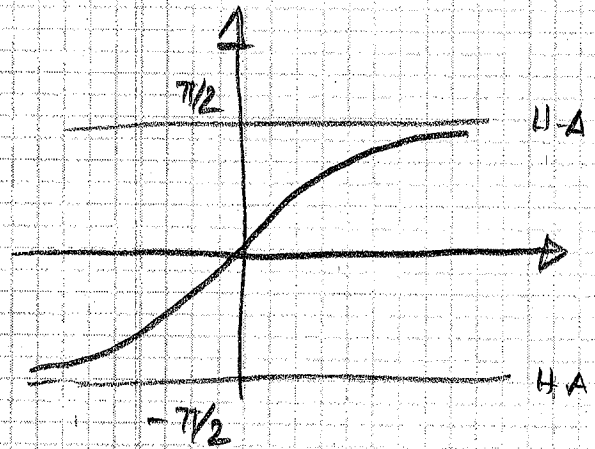


# THE INVERSE TANGENT FUNCTION



not one-to-one.



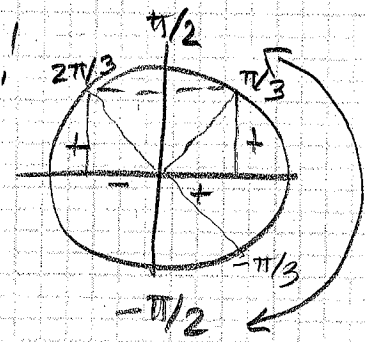
Domain =  $(-\infty, \infty)$

Range =  $(-\pi/2, \pi/2)$

$\tan^{-1}(\tan x) = x$  if  $-\pi/2 \leq x \leq \pi/2$   
 $\tan(\tan^{-1} x) = x$  if  $x$  is any real number

Ex:  $\tan^{-1}(\tan(\pi/3)) = \pi/3$ ? Yes!

Ex:  $\tan^{-1}(\tan(2\pi/3)) = 2\pi/3$ ? No.



$$\begin{aligned} \tan\left(\frac{2\pi}{3}\right) &= -\tan\left(\frac{\pi}{3}\right) = \\ &= \tan\left(-\frac{\pi}{3}\right) \end{aligned}$$

$-\tan(x) = \tan(-x)$   
odd

$$\Delta \tan^{-1}(\tan(-\pi/3)) = -\pi/3$$